

## INVESTIGATION OF THE EFFECT OF SOLUTION DESTABILIZATION ON FLUX ENHANCEMENT IN FILTRATION

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### Summary

A simple model for the filtration of a destabilized colloidal suspension is proposed. It takes into account the effect of flocculation on the properties of the deposited layer. It is shown that the cake permeability is a function of the quantity  $\omega t_R$ , where  $\omega$  is the flocculation rate (collision frequency) and  $t_R$  is the residence time defined by the time from which the particle enters the membrane channel to the time that it attaches onto the membrane surface.

### Introduction

According to the classical constant-pressure filtration theory, the rate of flux decline,  $\partial v_w / \partial t$ , at short times (i.e., while  $\Delta v_w / v_w \ll 1$  so that the flux reduces linearly with time) is directly proportional to the solids volume fraction,  $\phi$ , in the feed. The relation is given by

$$\lim_{t \rightarrow 0} \frac{\partial v_w}{\partial t} = \frac{v_w^2}{(1 - \epsilon) R_m k_f} \phi \quad (1)$$

where  $\phi$  is proportional to the particle number density for a unimodal distribution,  $v_w$  is the solvent permeation velocity or the solvent flux per unit membrane area,  $\epsilon$  is the effective cake porosity or void volume fraction,  $R_m$  is the membrane hydrodynamic resistance to flow, and  $k_f$  is the cake permeability. Disagreements, however, with the above-mentioned linear characteristic can be observed if the colloidal solution is destabilized in order to promote rapid colloid coagulation.

Figure 1 clearly identifies such a situation. Obtained from Cohen and Probstein [1], it represents a series of experiments carried out under identical flow, pressure, and temperature conditions, but different solution stability criteria. It should be mentioned that the ordinate of Figure 1,  $\alpha$ , which is defined as the "specific transmembrane force", is directly related to the rate of flux decline,  $\partial v_w / \partial t$  (see Ref. [1]). Here, the disagreement with eqn. (1) is clearly repre-